

## Displacements from gravimetry

For double-integration of acceleration, see <http://froste.oso.chalmers.se/hgs/SCG/g2d.html>

$$dg := \partial_t \partial_t s + (\partial_s g) s + (\psi / r) (n+1) k$$

Frame acceleration is big. But we have also a  $dg$  due to the displacement in the gravity gradient, and another  $dg$  due to mass redistribution. Assume that these terms are due to a tide-like potential designated by  $\psi$  ( $\psi$ ) under free-surface boundary conditions, and assume further that we may neglect whether or not the earth model is computed with inertial terms (which is a severe problem in the case of normal-mode overtones, but \*hopefully\* not in the case of the zero-tone).

In the above,  $r$  is earth radius and  $g$  normal gravity.

With Love numbers  $h$  and  $k$  pertaining to spherical harmonic degree  $n$ :

$$\text{In[4]} := s := (\psi / g) h$$

$$(\partial_s g) := -2g / r$$

$$(\partial_s g) s := 2h (\psi / r)$$

$$\text{In[3]} := \psi := s g / h$$

$$dg := \partial_t \partial_t s + (\partial_s g) s + (g / r) (n+1) (k / h) s$$

$$dg := \partial_t \partial_t s - (2g / r) s + (g / r) (n+1) (k / h) s$$

The wavelength in a Rayleigh-wave from Maule is ~200 km.

The wavenumber is then  $40000/200 = \sim 200$

The Normal Mode  ${}_0S_4$  at 0.65 mHz:  $\omega^2 = 17 \text{ nm/s}^2 / \text{mm}$

The acceleration is

$$dg = (-\omega^2 10^6 - \{3.01 (1 - (n+1) k_n / (2 h_n))\}) s$$

where  $s$  is the displacement amplitude in mm and  $dg$  is in  $\text{nm} / \text{s}^2$ .

$$\text{Conversely, if you know } dg, s = -\frac{dg}{10^6 \omega^2 + \{ \}}$$

which invites to compute the conversion in the Fourier domain. Get the curly bracket using (froste: cd ~hgs/Maxwell ):

```
elastic-list -fprem_l121_um0.7_lm10.n1-200 -12,200 -u | awk '\!/</{print $1,3.01*(($1+1)*$3/$2/2-1)}'
```

At  ${}_0S_4$  the curly bracket is worth ~10% of the acceleration term, more exactly  $-1.23 \text{ nm/s}^2 / \text{mm}$

It's allmost certain that Rayleigh waves are not well represented by high-wave-number tidal Love numbers. However, in the case of the ~1 min periods, the elastic-earth contributions can be safely neglected. Then, the displacement can be

approximated well with a double time integration.

$$4 \pi^2 (0.00065)^2 10^6 (* \text{nm/s}^2 / \text{mm} *)$$

Out[7]= 16.6796